AMATYC

STUDENT MATHEMATICS LEAGUE TEST #3

INSTRUCTIONS FOR ANSWER SHEET

TO THE STUDENT:

You have one hour to take this test. Scratch paper, which will be supplied, is allowed. Also allowed are calculators, including graphics calculators, provided they do not have a typewriter-like keyboard (such as, for example, the TI-92) or a disk drive. However, no books, mathematical tables, computers, or questions are permitted during the test.

You are NOT expected to be able to answer all the questions; do not become discouraged at the difficulty of the questions. Do not waste too much time on one question, but return to it after you finish the others.

Each question has a 2 point value for a correct answer and a penalty of -1/2 point for each wrong answer. There is no deduction for unanswered questions or for wrong answers to questions which are not multiple choice. Do not make any random guesses, but do answer a question if you can eliminate some of the choices.

Put the letter for the best response to each question you answer in the first column on the answer sheet provided.

Are there any questions?

Do not begin until you are told to do so.

1. Which of the following has as its graph a parabola which opens left?

A.
$$2y^2 = 11 - 3x$$

A.
$$2y^2 = 11 - 3x$$
 B. $5x = 13 + 2y^2$

C.
$$3y = 7 + 4x^2$$

D.
$$3x^2 = 8 - 2y$$

E.
$$x^2 = 10 - y^2$$

2. If three distinct counting numbers have a sum of 10 and a product of 20, then what is their median?

- E. There is not enough information given.
- 3. If L is a straight line passing through (8,11) with slope -3, then what is the ycoordinate of the intersection of L with the line x = 5?

- E. none of these
- 4. If one root of $3x^2 + j = kx$ is $2 + \sqrt{3}$, where j and k are rational, then j + k =

- E. none of these
- 5. If AB is the diameter of a circle, and C is on the circle such that $\overline{AC} = 10$ and $\overline{BC} = 16$, then the area of the circle is

B.
$$2\pi\sqrt{89}$$

- E. none of these
- 6. If the solution set for f(x) < 3 is $(0,+\infty)$, and the solution set for f(x) > -2 is

$$(-\infty,5)$$
, then the solution set for $[f(x)]^2 \ge f(x) + 6$ is

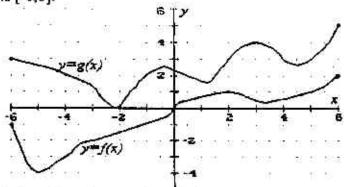
A.
$$(-\infty, +\infty)$$

C.
$$(-\infty, 0]$$
 D. $[5, +\infty)$

E.
$$(-\infty,0]\cup[5,+\infty)$$

7. If (a,b) is a solution for $2a+3b \le 12$ and $5a+2b \le 20$, where a and b are nonnegative integers, then the maximum possible value of a + b is

Questions 8-10 refer to the functions f and g, whose graphs are shown below and whose common domain is [-6,6].



8. How many solutions does the equation g(x) = 2 have?

A. 0

- B. 1
- C. 2
- D. 3
- E 4
- 9. How many solutions does the equation g(x) = |f(x)| have?

- B. 1
- C. 2
- D. 3
- E. 4
- 10. Suppose that g is the restriction to [-6,6] of a periodic function G whose domain is is $(-\infty,+\infty)$ and whose period is 16. The approximate value of G(100) is

A. 0

- B. 2
- C. 2.3
- D. 3
- E. 5

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11.	Each of six balanteach face (giving are rolled (like of AMATYC can be cubes? (M, T, Y A. 0.03	g each cube to lice), what is to be spelled by a	vo faces wi the probabil arranging th	th indistir lity, round le letters e; A musi	nguishab ded to to that app	ole A's). wo decim ear on th	If the six al places, e top face	cubes that
12.	A geometric seq the third term?	uence has a fi	rst term of	tan / and	а сопп	on ratio	of 2 cost.	What is
	A. 4 siπ t	B. 2 sin 21	C.	4 sec t	D.	4 cos 21	E. 4	tcos² t
13.	Two straight line $m \neq n$. The line of the origin. The s A2	of slope m has	y-intercept sible values	m, and t	he line o	he point of slope n	(m,n), who passes the	ere rough
1	Albert goes into I will spend \$20 does the same thi time, and Albert s total of his debt to A. \$48.50	in your store." ng at a second spending \$20	" The own I, third, and each time. re owners?	er agrees I fourth s	and Al tore, wi Albert	bert spen th the ow	ds \$20. A	albert ing each nat is the
15	$If x^4 + 5x^2 - 19$							
RELATI	A. 95					D. 0		of these
	Suppose all of th wheels on 5 axle 88 axles pass by.	e vehicles trav s or 4 wheels How many v	eling on a	certain in es. In a f	iterstate ive mini	highway ite period? it period?	have either, 224 who	er 18
	Half the reciproc the least integer to A. 1 B.		er than ten	times the		?	number.	What is
	There are 100 U. chosen at randon given state is rep A. 0.29	n, what is the resented?	probability	ach of the (rounded	: 50 stat i to two	es, If 20 decimal	places) th	
19.	Suppose $a > 0$. A. $-1 + \log_a$	Solve for x : $a\left(\frac{3}{2}\right) \qquad B$	$a^{3s+1} = 2a^s$ $-1 + \log$					
	D. $\log_a \sqrt{3}$		10073					
20.	A picket fence ha	s 100 vertica	boards, nu	imbered	I through	h 100 A	any board	whose

20. A picket fence has 100 vertical boards, numbered 1 through 100. Any board whose number is of the form 2k-1 is painted red (1,3,5,7,...,99). Next any unpainted board whose number is of the form 3k-1 is painted blue (2,8,14,...,98). If this process is continued, by increasing the coefficient of k by one and choosing a different color at each step, how many colors will be on the fence when every board has been painted?

A. 26

B. 29

C. 32

D. 35

E. none of these

NAME	Key	Tosz 3	COLLEGE		
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	Student's Responses	Local Corrector	
1	Α		# correct =
2	. с		# incorrect =
3	D	1.00	# blank
4	D	00 Ur	
5	Α	10785	
6	E		= # correct × 2
7	D	Si Si	
8	ш		_ # wrong × ½
9	C	10.2100	722.2
10	D		
11	A		= score
12	8	0	5 (5)
13	E		
14	C		r V
15	A	ena boronessa no	* V
16	E		
17	В		73. N
18	D		
19	С		5 5
20	A	\$7.	